# Cumulativity in Right Node Raising Construction* 

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## 1 Introduction

This paper argues for a so-called movement parse of right node raising construction (RNR, Ross 1967). RNR is typically a coordination construction which features a rightmost constituent shared by the two coordinates (1). ${ }^{1}$
(1) a. Abe boiled and Bert fried, these 50 dumplings.
b. [[Abe boiled $\left.\mathrm{t}_{1}\right]$ and [Bert fried $\left.\left.\mathrm{t}_{1}\right]\right]$ [these 50 dumplings $]_{1}$. Movement parse

- (1b): The movement parse posits rightward across-the-board (ATB) movement of the shared item, these 50 dumplings.

The literature provides mainly two types of arguments for the movement parse.

- Various movement constraints are operative in RNR formation (e.g., Bresnan 1974, Postal 1998, Sabbagh 2007).
- The shared item can be interpreted as outscoping the coordination (e.g., Jackendoff 1977, Sabbagh 2007).

As an instance of the second type of arguments, this paper investigates how RNR derives so-called cumulative readings or cumulative relation/cumulativity.

[^0]
## Goal:

- Demonstrate that the availability of cumulative readings supports the movement parse.
- Hirsch and Wagner (2015) sketch how RNR derives cumulativity. But their analysis undergenerates with respect to a particular RNR with a cumulative reading.
- Following Schmitt (2019), this paper presents a new analysis of cumulativity/plurals that can capture cumulative readings in a wider range of RNR than Hirsch and Wagner's analysis.


## Organization:

Section 2: Define cumulative readings.
Section 3: Introduce three parses of RNR.
Section 4: Discuss Hirsch and Wagner's analysis of cumulative readings in RNR.
Section 5: Present this paper's analysis of cumulative readings.
Section 6: Demonstrate that under the proposed analysis of cumulativity, the movement parse can derive cumulativity in a wide range of RNR.
Section 7: Conclude.

## 2 Cumulativity

This section defines cumulativity with respect to RNR as in (1).
Schmitt (2019) shows that cumulativity can be observed in sentences with two plurals of various semantic types, as exemplified in (2).
(2) a. [A Abe and Bert] [ ${ }_{B}$ sank and fell]
b. Cumulative reading:

Each of Abe and Bert sank or fell and each incident (i.e., sinking and falling) happened to Abe or Bert.

Cumulative readings can be characterized by sentences' truth conditions that refer to particular binary relations between two plurals (see Scha 1981, Link 1983, Krifka 1986 a.o.), as shown in (3) for cumulativity as in (2).
(3) 1 iff $\forall \mathrm{x} \in \mathrm{S}_{A} \exists \mathrm{f} \in \mathrm{S}_{B} \mathrm{f}(\mathrm{x})=1 \wedge \forall \mathrm{f} \in \mathrm{S}_{B} \exists \mathrm{x} \in \mathrm{S}_{A} \mathrm{f}(\mathrm{x})=1$
( $\mathrm{S}_{A}$ and $\mathrm{S}_{B}$ are sets of objects that plurals A and B consist of intuitively.)
(Schmitt 2019, 8)
With (3) in mind, consider again the RNR in (1), repeated below as (4).
(4) a. [ $A_{A}$ Abe boiled and Bert fried], [ ${ }_{B}$ these 50 dumplings].
b. Cumulative reading:

Abe boiled some of these 50 dumplings, Bert fried some of these 50 dumplings, and each dumpling was boiled by Abe or fried by Bert.

The truth condition of the cumulative reading can be represented in the form of (3) (5).
(5) 1 iff $\forall \mathrm{x} \in\left\{\mathrm{D}_{1}, \ldots, \mathrm{D}_{50}\right\} \exists \mathrm{f} \in\{$ Abe-boiled', Bert-fried $\} \mathrm{f}(\mathrm{x})=1 \wedge$
$\forall f \in\{$ Abe-boiled', Bert-fried $\} \exists \mathrm{x} \in\left\{\mathrm{D}_{1}, \ldots, \mathrm{D}_{50}\right\} \mathrm{f}(\mathrm{x})=1$

- Abe-boiled'/Bert-fried': the two properties that A consists of intuitively.
- $D_{1}, \ldots, D_{50}$ : contextually salient 50 dumplings that B consists of intuitively.

To sum up, this section defined cumulativity, and showed RNR as in (4) derives cumulativity.

## 3 Three parses of RNR

This section introduces two parses of RNR other than the movement parse, and demonstrates that they do not seem to derive cumulativity in RNR unlike the movement parse.

## Ellipsis parse:

The ellipsis parse posits backwards PF deletion in the first conjunct, as shown in (6) for (4) (e.g., Wexler and Culicover 1980, Hartmann 2001, An 2007, Ha 2008).
(6) Abe boiled these 50 dumplings and Bert fried these 50 dumplings.

- The ellipsis parse only derives distributivity, just like its purported source sentence.
- In each conjunct, these 50 dumplings does not have a plural to cumulatively compose with.


## Multi-dominance parse:

The multi-dominance parse, sketched in (7) for (4), posits that the shared item is literally shared by two conjuncts (e.g., Wilder 1999, Bachrach and Katzir 2009a, Grosz 2015).


- If the shared item is interpreted as an object of boiled and fried in each conjunct separately, the multi-dominance parse also derives only the distributive reading.

In fact, Grosz (2015) assumes that a shared item in RNR is interpreted in each conjunct separately. Thus, at least his multi-dominance analysis does not predict the presence of cumulativity in RNR.

## Movement parse:

The movement parse of (4) is sketched in (8).


At first sight, the movement pare also seems to derive only distributivity. For example, consider the composition in (8) under the Boolean analysis of English and.

- $\llbracket \& \mathrm{P}_{1} \rrbracket=1$ iff Abe boiled $\mathrm{g}(1) \wedge$ Bert fried $\mathrm{g}(1)($ where $1 \in \operatorname{dom}(\mathrm{~g}))$
- $\llbracket \& \mathrm{P}_{2} \rrbracket=\lambda \mathrm{x}_{e}$.Abe boiled $\mathrm{x} \wedge$ Bert fried x
- $\llbracket \& \mathrm{P}_{3} \rrbracket=1$ iff Abe boiled $\llbracket$ these 50 dumplings $\rrbracket \wedge$ Bert fried $\llbracket$ these 50 dumplings $\rrbracket$.

However, consider the non-RNR sentence in (9), which can denote a cumulative reading and structurally resembles (8).
(9) [Abe and Bert $]_{1}\left[\left[V P\right.\right.$ sank $\left.\mathrm{t}_{1}\right]$ and $\left[{ }_{V P}\right.$ fell $\left.\left.\mathrm{t}_{1}\right]\right]$
non-RNR

- The sentence involves a propositional conjunction and a plural DP that has ATB moved from the conjuncts as in (8).
- Whatever mechanism derives the cumulativity in (9) is likely to derive the cumulativity in (8). ${ }^{2}$

To sum up, while the three parses of RNR can all derive distributive readings, only the movement parse seems to be compatible with the availability of cumulative readings.

Question: Can the movement parse indeed derive cumulativity?
I will positively answer this question. We will first observe a previous compositional analysis of cumulativity in RNR.

[^1](1) a. Abe boiled and Bert fried, these $\mathbf{5 0}$ dumplings.

RNR
b. Which dumplings did Abe boil and Bert fry?
wh-question
c. These 50 dumplings, Abe boiled and Bert fried.

Topic sentence
Interestingly, while (1b) allows a cumulative reading, (1c) does not. I leave the lack of cumulativity in topic sentences for future research.

## 4 Hirsch and Wagner (2015)

### 4.1 Cumulative derivation

Hirsch and Wagner (2015) sketch an analysis of how cumulativity is derived in RNR in (4) based on two assumptions.

Assumption 1: English and is optionally analyzed as a non-Boolean and.
The non-Boolean and can be defined as the type-polymorphous $\sqcup$ in (11), which is based on the notion of e-conjoinable types (10).
(10) e-conjoinable types
$e$ is an e-conjoinable type and if $\mathrm{a}_{1}, \ldots, \mathrm{a}_{n}$ are e-conjoinable types, then $\left(\left(\mathrm{a}_{1}\right) \ldots\left(\mathrm{a}_{n}\right) \mathrm{t}\right)$ is an $e$-conjoinable type.
(Schmitt 2019, 12)
(11)

$$
\mathrm{X} \sqcup \mathrm{Y}=\left\{\begin{array}{l}
\mathrm{X} \oplus \mathrm{Y} \text { if } \mathrm{X}, \mathrm{Y} \in \mathrm{D}_{e} \\
\lambda \mathrm{Z}_{a} \cdot \exists \mathrm{Z}, \mathrm{Z}^{\prime \prime}\left[\mathrm{Z}=\mathrm{Z}^{\prime} \sqcup \mathrm{Z} " \wedge \mathrm{X}\left(\mathrm{Z}^{\prime}\right) \wedge \mathrm{Y}\left(\mathrm{Z}^{\prime \prime}\right)\right] \\
\text { if } \mathrm{X}, \mathrm{Y} \in \mathrm{D}_{<a, t>} \text { and }<a, \mathrm{t}>\text { is e-conjoinable } \\
\lambda \mathrm{Z}^{1}, \ldots, \mathrm{Z}^{n} \cdot \exists \mathrm{Z}^{1}, \mathrm{Z}^{1 "}, \ldots, \mathrm{Z}^{n^{\prime}}, \mathrm{Z}^{n^{\prime \prime}}\left[\mathrm{Z}^{1}=\mathrm{Z}^{1^{\prime}} \sqcup \mathrm{Z}^{1 "} \wedge \ldots \wedge \mathrm{Z}^{n}=\mathrm{Z}^{n^{\prime}} \sqcup \mathrm{Z}^{n^{\prime \prime}}\right. \\
\left.\wedge \mathrm{X}\left(\mathrm{Z}^{1^{\prime}}\right) \ldots\left(\mathrm{Z}^{n^{\prime}}\right) \wedge \mathrm{Y}\left(\mathrm{Z}^{\prime \prime}\right) \ldots\left(\mathrm{Z}^{n^{\prime \prime}}\right)\right] \\
\text { if } \mathrm{X}, \mathrm{Y} \in \mathrm{D}_{<a_{1}<\ldots<a_{n}, t>\ldots \gg} \text { and }<a_{1}<\ldots<a_{n}, \mathrm{t}>\ldots \gg \text { is e-conjoinable. }
\end{array}\right\}
$$

(Schmitt 2019, 12)
To understand how the non-Boolean and works, consider (12).
(12) $\left[\begin{array}{l}\text { A Abe and Bert }][B \text { sank and fell }] ~\end{array}\right.$

- «Abe and Bert』 $=$ Abe $\oplus$ Bert- 【sank and fell $\rrbracket=\lambda \mathrm{x}_{e} \cdot \exists \mathrm{y}, \mathrm{z}\left[\mathrm{x}=\mathrm{y} \oplus \mathrm{z} \wedge \operatorname{sank}^{\prime}(\mathrm{y}) \wedge\right.$ fell' $\left.(\mathrm{z})\right]$
- $\llbracket(12) \rrbracket=1$ iff $\exists \mathrm{y}, \mathrm{z}\left[\right.$ Abe $\oplus$ Bert $=\mathrm{y} \oplus \mathrm{z} \wedge \operatorname{sank}^{\prime}(\mathrm{y}) \wedge$ fell $\left.^{\prime}(\mathrm{z})\right]$

Importantly, the non-Boolean and encodes cumulativity in its meaning.
Assumption 2: The movement of a shared item introduces one binder index in each conjunct. Under this assumption, the movement parse of the RNR in (13a) can be illustrated as in (13b).
a. Abe boiled and Bert fried these 50 dumplings.
b.


- There is a binder index 1 under $\mathrm{TP}_{2}$ and $\mathrm{TP}_{4}$.


## Cumulative derivation in (13a):

Based on the two assumptions above, Hirsch and Wagner (2015) explain how cumulativity is derived in (13a).

- $\llbracket \mathrm{TP}_{1} \rrbracket=1$ iff Abe boiled $\mathrm{g}(1)$
$=$ Abe-boiled'
Abbreviation
- $\llbracket \mathrm{TP}_{2} \rrbracket=$ Bert-fried ${ }^{\prime}$
- $\llbracket \& \mathrm{P}_{1} \rrbracket=\lambda \mathrm{x}_{e} \cdot \exists \mathrm{y}, \mathrm{z}\left[\mathrm{x}=\mathrm{y} \oplus \mathrm{z} \wedge\right.$ Abe-boiled' $(\mathrm{y}) \wedge$ Bert-fried $\left.^{\prime}(\mathrm{z})\right]$
- $\llbracket \mathrm{DP} \rrbracket=\mathrm{D}_{1} \oplus \ldots \oplus \mathrm{D}_{50}$
- $\llbracket \& \mathrm{P}_{2} \rrbracket=1$ iff $\exists \mathrm{y}, \mathrm{z}\left[\mathrm{D}_{1} \oplus \ldots \oplus \mathrm{D}_{50}=\mathrm{y} \oplus \mathrm{z} \wedge\right.$ Abe-boiled' $\left.^{\prime}(\mathrm{y}) \wedge \operatorname{Bert-fried}^{\prime}(\mathrm{z})\right]$


### 4.2 Undergeneration problem

Hirsch and Wagner's analysis do not appear to derive cumulativity in RNR as in (14), where the shared item itself is not a plural but involves a plural.
a. John says $\left[\left[\right.\right.$ that Friederike must $\mathrm{t}_{1}$ ] and [that Konrad may $\left.\mathrm{t}_{1}\right]$ ], [record two quite different songs $]_{1}$.
(Abels 2004, 9)
b. [[Abe got his Ph.D. $\mathrm{t}_{1}$ ] and [Bert got his MA $\mathrm{t}_{1}$ ]] [from these two universities $]_{1}$

- (14b) can mean that Abe got his Ph.D. from one of these two universities and Bert got his MA from the other university.

Hirsch and Wagner's analysis predicts that the RNR in (14) is limited to denoting a distributive reading, as shown in (15).


- $\llbracket \mathrm{PP} \rrbracket=$ from $-\mathrm{A} \oplus \mathrm{B}^{\prime}$
- $\llbracket \mathrm{TP}_{1} \rrbracket=1$ iff $\operatorname{got}^{\prime}($ his Ph.D. $)(\mathrm{g}(1))(\mathrm{Abe})=1$
(assumption: $\mathrm{t}_{1}$ is a higher type trace)
- $\llbracket \mathrm{TP}_{2} \rrbracket=\lambda \mathrm{f}_{e t}$.got'(his Ph.D.)(f)(Abe) $=1$
- $\llbracket \mathrm{TP}_{4} \rrbracket=\lambda \mathrm{f}_{e t}$. got' $($ his MA) $(\mathrm{f})($ Bert $)=1$
- $\llbracket \& \mathrm{P}_{1} \rrbracket=\lambda \mathrm{f}_{e t} \cdot \exists \mathrm{P}, \mathrm{Q}[\mathrm{f}=\mathrm{P} \oplus \mathrm{Q} \wedge$ got' $($ his Ph.D. $)(\mathrm{P})(\mathrm{Abe}) \wedge$ got'(his MA)(Q)(Bert)]
- $\llbracket \& \mathrm{P}_{2} \rrbracket=1$ iff $\exists \mathrm{P}, \mathrm{Q}\left[\right.$ from- $\mathrm{A} \oplus \mathrm{B}^{\prime}=\mathrm{P} \oplus \mathrm{Q} \wedge \operatorname{got}^{\prime}($ his Ph.D. $)(\mathrm{P})(\mathrm{Abe}) \wedge$ got'(his MA)(Q)(Bert)]


## Problem of Hirsch and Wagner's analysis:

- The shared item does not serve as a plural even if it involves a plural. ${ }^{3}$


## Solution:

- We devise a mechanism by which a plurality (e.g., these two university in (14b)) "projects" to its embedding expression (e.g., from these two university in (14b)).
- Schmitt (2019) proposes such a mechanism.
- The next section presents a different analysis of cumulativity, following Schmitt (2019).

The analysis to be proposed adopts all the central tenets of Schmitt's analysis, but departs from her analysis in compositional details.

## 5 Analysis of cumulativity

This section presents a new analysis of cumulativity following Schmitt (2019). Given that cumulativity is a particular binary relation between two plurals, an analysis of cumulativity can be divided into:

[^2]－an analysis of plurals（Section 5．1）
－how they compose together to yield cumulativity（Section 5．2）

## 5．1 Plural set derivation

This paper adopts：
－Intentional semantics（e．g．，Lewis 1976）
e．g．，$\llbracket \operatorname{sink} \rrbracket=\lambda \mathrm{w}_{s} \cdot \lambda \mathrm{x}_{e} \cdot \mathrm{x} \operatorname{sinks}$ in $\mathrm{w}\left(=\operatorname{sink}{ }^{\prime}\right)$
$\llbracket$ boil】 $=\lambda \mathrm{w}_{s} \cdot \lambda \mathrm{x}_{e} \cdot \lambda \mathrm{y}_{e} \cdot \mathrm{y}$ boils x in $\mathrm{w}\left(=\right.$ boil $\left.^{\prime}\right)$
－Hamblin semantics
e．g．，$\llbracket \mathrm{Abe} \rrbracket=\{\mathrm{Abe}\}$
$\llbracket \operatorname{sink} \rrbracket=\left\{\operatorname{sink}{ }^{\prime}\right\}$
$\llbracket$ Abe sank $\rrbracket=\{$ Abe sank $\}$
－Schmitt＇s cross categorical plurality ${ }^{4}$
e．g．，【Abe and Bert $\rrbracket / \llbracket$ the two students $\rrbracket=\{$ Abe，Bert $\}$
when the contextually salient students are Abe and Bert．
$\llbracket$ sink and fall】 $=\{$ sink＇，fall＇$\}$
$\llbracket$ Abe sank and Bert fell】 $=\{$ Abe sank，Bert fell $\}$
－The conjunctive effect of and is due to a separate operator that makes use of the alter－ natives in plural sets（see Winter 1995 for a related analysis）．

## 5．2 Plural set composition

This section explains how sets in a Hamblin semantics undergo semantic compositions，deriving cumulativity in non－RNR sentences．Consider first the simple sentence with a DP conjunction in（16a）and its structure in（16b）．
（16）a．Abe and Bert sank．
b．


[^3]\[

$$
\begin{aligned}
& \llbracket \mathrm{TP}_{1} \rrbracket=\{\text { Abe sank, Bert sank }\} \\
& \llbracket \sqcap \rrbracket=\lambda \mathrm{p}_{s t}\left\{\lambda \mathrm{w}_{s} \cdot \forall \mathrm{p}_{s t} \cdot\left[\mathrm{p} \in \llbracket \beta \rrbracket^{g} \rightarrow \mathrm{p}(\mathrm{w})=1\right]\right\} \\
& \llbracket \mathrm{TP}_{2} \rrbracket=\left\{\lambda \mathrm{w}_{s} \cdot \forall \mathrm{p}_{\text {st }} \cdot[\mathrm{p} \in\{\text { Abe sank, Bert sank }\} \rightarrow \mathrm{p}(\mathrm{w})=1]\right\}
\end{aligned}
$$
\]

## (17) Point-wise Functional Application (PFA)

If $\alpha$ is a branching node whose daughters are a $\beta$ and $\gamma$, and $\llbracket \beta \rrbracket^{g} \subseteq \mathrm{D}_{\sigma}$ and $\llbracket \gamma \rrbracket^{g} \subseteq \mathrm{D}_{\sigma \iota}$, then $\llbracket \alpha \rrbracket^{g}=\left\{\mathrm{f}(\mathrm{x}): \mathrm{f} \in \llbracket \gamma \rrbracket^{g}\right.$ and $\left.\mathrm{x} \in \llbracket \beta \rrbracket^{g}\right\}$
(adapted from Kratzer and Shimoyama 2017, 127)

( $f$ and $g$ are functions of type $\langle\sigma \iota\rangle$ and $x$ and $y$ are their arguments of type $<\sigma>$.)

- PFA enables the plurality of an expression to be projected to its embedding expression.

Next, we turn to the sentence with a predicate conjunction in (18). ${ }^{5}$
a. Abe sank and fell.
b.


$$
\begin{aligned}
\llbracket \mathrm{T}^{\prime}{ }_{1} \rrbracket^{g} & =\{\mathrm{g}(1) \text { sank, } \mathrm{g}(1) \text { fell }\} \\
\llbracket \mathrm{T}^{\prime}{ }_{2} \rrbracket^{g} & =\{\text { sank', fell' }\} \\
\llbracket \mathrm{TP}_{1} \rrbracket & =\{\text { Abe sank, Abe fell }\} \\
\llbracket \mathrm{TP}_{2} \rrbracket & =\left\{\lambda \mathrm{w}_{s} \cdot \forall \mathrm{p}_{s t} \cdot[\mathrm{p} \in\{\text { Abe sank, Abe fell }\} \rightarrow \mathrm{p}(\mathrm{w})=1]\right\}
\end{aligned}
$$

(19) Point-wise Predicate Abstraction (PPA) ${ }^{6}$

If $\alpha$ is a branching node whose daughters are an index i and $\beta$, where $\llbracket \beta \rrbracket^{g} \subseteq \mathrm{D}_{\sigma}$, then $\llbracket \alpha \rrbracket^{g}=\left\{\mathrm{f}: \mathrm{f} \in \mathrm{D}_{<e \sigma>} \& \forall a\left[\mathrm{f}(a) \in \llbracket \beta \rrbracket^{\left[g^{(a /]}\right]}\right\}\right.$
(Kratzer and Shimoyama 2017, 127)

$$
\begin{aligned}
& \left\{\underline{\lambda \mathbf{x}_{e}} \cdot \lambda \mathrm{w}_{s} . \ldots \underline{\mathbf{x}} \ldots, \underline{\lambda \mathbf{x}_{e}} \cdot \lambda \mathrm{w}_{s} . \ldots \underline{\mathbf{x}} \ldots, \ldots\right\}
\end{aligned}
$$

[^4]Composition of 1 and $\mathrm{T}_{1}$ in (18)
$\left\{\underline{\lambda \mathbf{x}_{e}} \cdot \lambda \mathrm{w}_{s} \cdot \underline{\mathbf{x}}\right.$ sank in w, $\underline{\mathbf{x}}_{e} \cdot \lambda \mathrm{w}_{s} \cdot \underline{\mathbf{x}}$ fell in w$\} /\left\{\right.$ sank' $^{\prime}$, fell' $\}$
$1\left\{\lambda \mathrm{w}_{s} \cdot \mathbf{g ( 1 )}\right.$ sank in $\mathrm{w}, \lambda \mathrm{w}_{s} \cdot \mathbf{g ( 1 )}$ fell in w$\} /\{\mathrm{g}(1)$ sank, $\mathrm{g}(1)$ fell $\}$
Finally, we turn to a non-RNR sentence with cumulativity (21).
(21) Abe and Bert sank and fell.

$$
\begin{align*}
& \llbracket \text { Abe and Bert } \rrbracket=\{\text { Abe, Bert }\} \\
& \llbracket \text { sank and fell } \rrbracket=\{\text { sank', fell' }\} \tag{18b}
\end{align*}
$$

To derive a cumulation between \{Abe, Bert \} and \{sank', fell'\}, this paper assumes a Cuml operator which takes two plural sets and returns a singleton set of a proposition.

$\llbracket \mathrm{Cuml} \rrbracket=\lambda \mathrm{X} . \lambda \mathrm{Y} .\left\{\lambda \mathrm{w}_{s} . \forall \mathrm{x} \in \mathrm{X} \quad \exists \mathrm{y} \in \mathrm{Y} \mathrm{x}(\mathrm{y})(\mathrm{w})=1 \& \forall \mathrm{y} \in \mathrm{Y} \quad \exists \mathrm{x} \in \mathrm{X} \mathrm{x}(\mathrm{y})(\mathrm{w})=1\right\}$
$\llbracket \mathrm{TP} \rrbracket=\left\{\lambda \mathrm{w}_{s} . \forall \mathrm{x} \in\left\{\right.\right.$ sank' $^{\prime}$, fell' $\} \exists \mathrm{y} \in\{$ Abe, Bert $\} \mathrm{x}(\mathrm{y})(\mathrm{w})=1$
$\& \forall y \in\{$ Abe, Bert $\} \exists \mathrm{x} \in\left\{\right.$ sank' $^{\prime}$, fell' $\left.\} \mathrm{x}(\mathrm{y})(\mathrm{w})=1\right\}$

## 6 Cumulativity in RNR

This section demonstrate that the movement parse can derive any types of cumulativity in RNR we have observed so far based on the the analysis of cumulativity in Section 5 .

We first adress the cumulativity in RNR with a shared DP in (23a).
a. Abe boiled and Bert fried these 50 dumplings.
b.


Abe boiled $\mathrm{t}_{1}$ and Bert fried $\mathrm{t}_{1}$
$\llbracket \& \mathrm{P}_{1} \rrbracket^{g}=\{$ Abe boiled $\mathrm{g}(1)$, Bert fried $\mathrm{g}(1)\}$
$\llbracket \& \mathrm{P}_{2} \rrbracket^{g}=\{$ Abe-boiled', Bert-fried' $\}$
«these 50 dumplings】 $=\left\{\mathrm{D}_{1}, \ldots, \mathrm{D}_{50}\right\}$
$\llbracket \& \mathrm{P}_{4} \rrbracket^{g}=\left\{\lambda \mathrm{w}_{s} . \forall \mathrm{x} \in\{\right.$ Abe-boiled', Bert-fried' $\} \exists \mathrm{y} \in\left\{\mathrm{D}_{1}, \ldots, \mathrm{D}_{50}\right\} \mathrm{x}(\mathrm{y})(\mathrm{w})=1$
$\& \forall y \in\left\{\mathrm{D}_{1}, \ldots, \mathrm{D}_{50}\right\} \exists \mathrm{x} \in\{$ Abe-boiled', Bert-fried' $\left.\} \mathrm{x}(\mathrm{y})(\mathrm{w})=1\right\}$

As for the distributive reading of (23a), we can derive it by composing $\& \mathrm{P}_{2}$ and DP in (23b) by the PFA, and applying $\square$ to the resulting set.

Next, we turn to the cumulativity in RNR with a shared T', which Hirsch and Wagner's analysis of cumulativity in RNR could not derive.
a. [[Abe got his Ph.D. $\mathrm{t}_{1}$ ] and [Bert got his MA $\left.\mathrm{t}_{1}\right]$ ] [from these two universities] ${ }_{1}$
b.


Abe got his Ph.D. $\mathrm{t}_{1}$ and Bert got his MA t $\mathrm{t}_{1}$
Suppose that these two universities refers to two universities $A$ and $B$.
$\llbracket \mathrm{PP} \rrbracket^{g}=\left\{\right.$ from $-\mathrm{A}^{\prime}$, from- B$\}$
$\llbracket \& \mathrm{P}_{1} \rrbracket^{g}=\left\{\right.$ got' $($ his Ph.D. $)(\mathrm{g}(1))($ Abe $)$, got' $^{\prime}($ his MA $)(\mathrm{g}(1))($ Bert $\left.)\right\}$
(assumption: $\mathrm{t}_{1}$ is a higher type trace)
$\llbracket \& \mathrm{P}_{2} \rrbracket^{g}=\left\{\lambda \mathrm{f}_{<e, s t>} \cdot \lambda \mathrm{W}_{s} . \operatorname{got}{ }^{\prime}(\right.$ his $\operatorname{Ph} . \mathrm{D}).(\mathrm{f})(\mathrm{Abe})(\mathrm{w})$,
$\lambda \mathrm{f}_{<e, s t\rangle} \cdot \lambda \mathrm{w}_{s}$. got'(his MA)(f)(Bert)(w) $\} \quad$ Revised PPA
$=\{$ Abe-got-his-Ph.D.', Bert-got-his-MA' $\}$ Abbreviation
$\llbracket \& \mathrm{P}_{4} \rrbracket^{g}=\left\{\lambda \mathrm{w}_{s} . \forall \mathrm{x} \in\{\right.$ Abe-got-his-Ph.D.', Bert-got-his-MA'\} $\exists \mathrm{y} \in\{$ from-A', from-B'\}
$\mathrm{x}(\mathrm{y})(\mathrm{w})=1 \& \forall \mathrm{y} \in\{$ from-A', from-B'\} $\exists \mathrm{x} \in\{$ Abe-got-his-Ph.D.',
Bert-got-his-MA'\} $\mathrm{x}(\mathrm{y})(\mathrm{w})=1\}$
(25) Revised Point-wise Predicate Abstraction (Revised PPA)

If $\alpha$ is a branching node whose daughters are an $\langle\mathrm{n}, \sigma\rangle$, where $n$ is a natural number and $\sigma$ is a semantic type, and $\beta$, where $[[\beta]]^{w, g} \subseteq \mathrm{D}_{\iota}$, then $[[\alpha]]^{w, g}=\left\{\mathrm{f}: \mathrm{f} \in \mathrm{D}_{<\sigma \iota\rangle} \& \forall a\right.$ $\left[\mathrm{f}(a) \in[[\beta]]^{\left.\left.w, g^{[a /<n, \sigma>]}\right]\right\}}\right.$

In this way, under this paper's analysis of cumulativity, the movement parse can derive cumulativity in (24) as well.

## 7 Conclusion

- The movement parse must be a possible structure for RNR.
- Among the three parses of RNR, only the movement parse can derive the cumulativity.
- The movement parse can also derive distributive readings of RNR which the other two parses derive.
- Based on Schmitt's analysis of cumulativity, I proposed a more straightforward analysis, which can still derive the same range of data as her analysis.
- It remains to be seen if an ellipsis or multi-dominance parse is still needed given that RNR is not subject to certain movement constraints (e.g., McCloskey 1986, Bachrach and Katzir 2009b) (see Abels 2004, Sabbagh 2007, Hirsch and Wagner 2015 for some discussions)


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    ${ }^{1}$ The acceptability judgements for the original data reported on this paper are those of several native speakers I consulted through questionnaires and informal interviews.

[^1]:    ${ }^{2}$ There are other types of sentences that structurally resemble the movement parse of RNR.

[^2]:    ${ }^{3}$ Any analysis of cumulativity which makes use of the non-Boolean and does not predict the availability of "long-distance" cumulativity (Schmitt 2019).

[^3]:    ${ }^{4}$ The ontology of pluralities other than plural individuals is proposed for different semantic types by several linguists（e．g．，Landman 2000，Beck and Sharvit 2002，Schlenker 2004，Gawron and Kehler 2004）．

[^4]:    ${ }^{5}(18 \mathrm{~b})$ is one of the possible structures. For instance, it is possible that $\Pi$ applies to \&P instead of $\mathrm{TP}_{1}$.
    ${ }^{6}$ See Shan (2004), Romero and Novel (2013), Charlow (2019) among others for discussion about the point-wise predicate abstraction defined in (19).

